

**Mossford Green's
Maths Calculation Booklet
Years 3-6**



This is the way we do it!

“They didn’t do it like that in my day!”

Do your children ask for help with their maths homework and start talking in a foreign language, using words like ‘partitioning’, ‘chunking’, ‘grid multiplication’.....?

If so, you may feel the need for some translation. This booklet is designed to explain some of the methods used to teach calculation in schools.

Which is more important:

mental calculation



written



This will depend on the numbers involved and the individual child.

When faced with a calculation, no matter how large or difficult the numbers may appear to be, all children should ask themselves:

Can I do this in my head?

If I can't do it wholly in my head, what do I need to write down in order to help me calculate the answer?

Do I know the approximate size of the answer?

Will the written method I know be helpful?



When do children need to start recording?

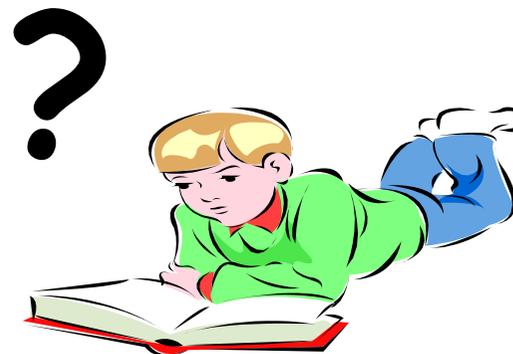
The following table shows how some sort of recording is relevant throughout the primary years with mental strategies playing an important role throughout.

Reception	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
← Making a record of a calculation →						
← Jotting to support a mental strategy →						
← Explaining a mental strategy →						
← Developing written methods →						

It is important to encourage children to look first at the problem and then get them to decide which is the best method to choose – pictures, mental calculation with or without jottings, structured recording or calculator.

Children attempting to use formal written methods without a secure understanding will try to remember rules, which may result in unnecessary and mistaken applications of a standard method.

$$\begin{array}{r} 24 \\ +39 \\ \hline 513 \end{array}$$



Some of the methods explained in this booklet involve 'partitioning' and a set of place value cards are attached which can be pasted onto card and cut out (your child will show you how to use them).

ADDITION

Prerequisite skills

Counting numbers to 20



Place numbers to 20 in order

Bonds up to 10 and to make 10



1 more than a number



Addition as combining groups



Doubling numbers within 20

Relate number bonds to 10 to add multiples of 10 up to a total of 100 e.g. if

$3 + 4$ is 7 then $30 + 40$ is 70



Use familiar objects to recognise the place value of 2 digit numbers.



Recognise and explain 24 is '2 tens and 4 ones'



Addition as counting on





Progressing to: PARTITIONING AND RECOMBINING
Partition into tens and ones and recombine Pre J10 (before jumping in 10s

$$\begin{aligned} 12 + 23 &= 10 + 2 + 20 + 3 \\ &= 30 + 5 \\ &= 35 \end{aligned}$$

As part of the early calculations policy, there are 3 ways for children to add numbers on a number line.

Jumping 10 – jumping in 10s and 1s
Targeting 10 – targeting a multiple of 10
O 10 – over jumping and adjusting

Jumping 10 – jumping in 10s and 1s

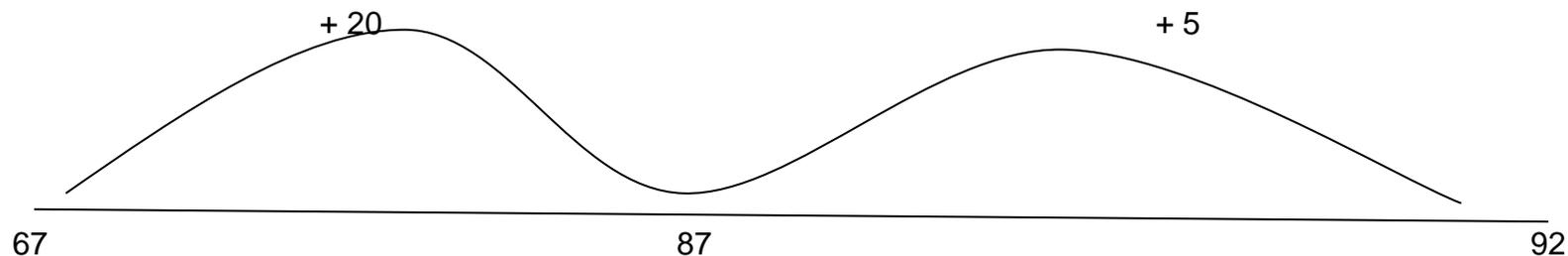
J10 – Jumping in 10s and 1s

This method involves starting with the largest number on the left of the number line. The small number is then partitioned and children jump, first adding the tens and then the units.

Children should write above the jump how much they are adding (e.g. +10, +1).

Once confident, children can progress to adding all the tens followed by all the units in one jump

$$67 + 25$$



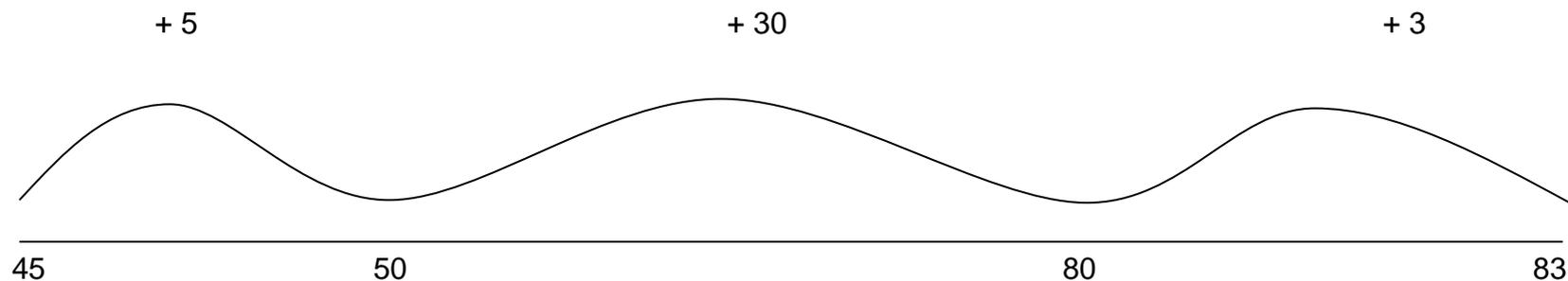
Once confident, children can progress to adding all the tens followed by all the units in one jump (eg + 50 + 2)

Target 10 – targeting a multiple of 10

T10 – Targeting a multiple of 10

Children use their knowledge of known facts to target the tens, starting with the largest number. They add whatever number is needed to reach the next multiple of ten and then add on whatever is remaining.

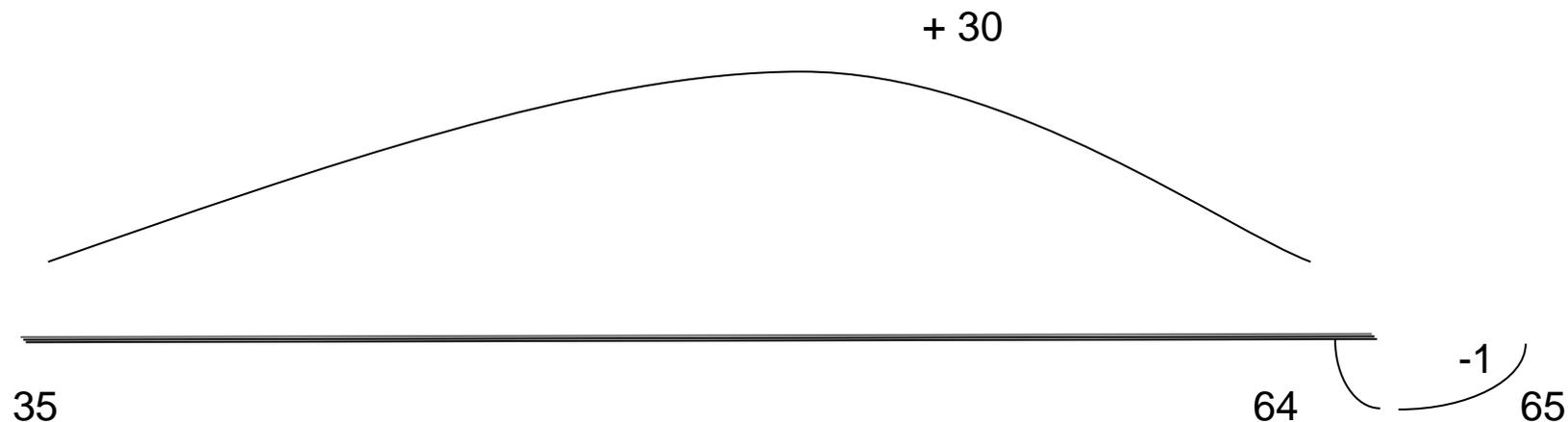
$$45 + 38$$



O10 – Over jumping and adjusting

This method would only really be used if one of the numbers ends in a 9 or a 1 (possibly a 8 or a 2). The round the number being added to the nearest multiple of ten and then jump by this amount along the number line. Adjustments would then be made by adding or subtracting (whichever is appropriate).

$$35 + 29$$



Using an informal method by counting on in multiples of 10 with a number line

Why use a number line?

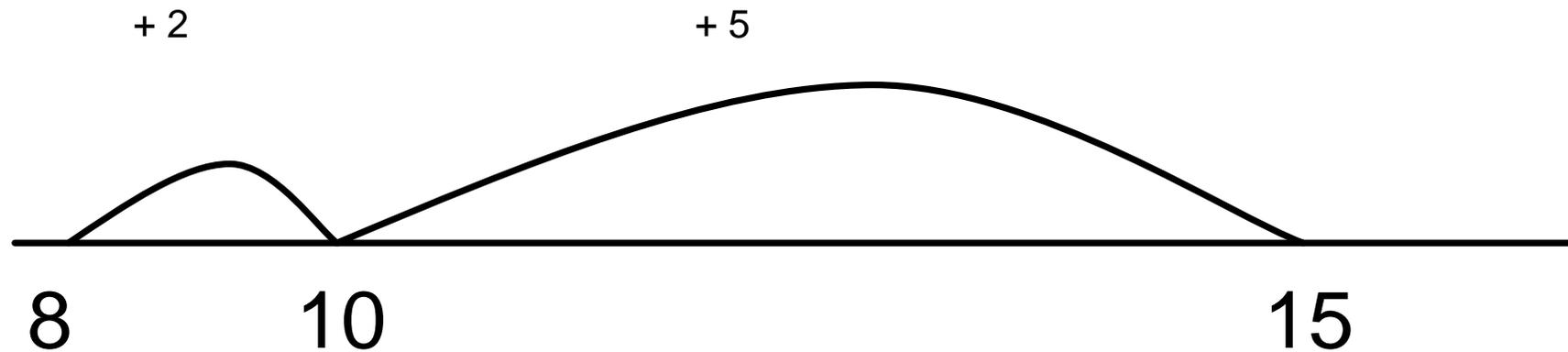
It helps me to show on paper what is going on in my head



Targeting 10

(Targeting the 10, partitioning and bridging through 10)

$$8 + 7 =$$



Children should be able to partition the 7 to relate adding the 2 first to target the 10 and then the 5.

ADDITION

Using a number

Number line to add too much and then subtract (Over 10)

HTU + TU

754 + 96

Why are you subtracting
when you should be
adding?

I noticed that 96 is close to 100.
100 is easier to add than 96 but
that means I've added 4 too
many. I need to subtract 4 from
the number I reach.

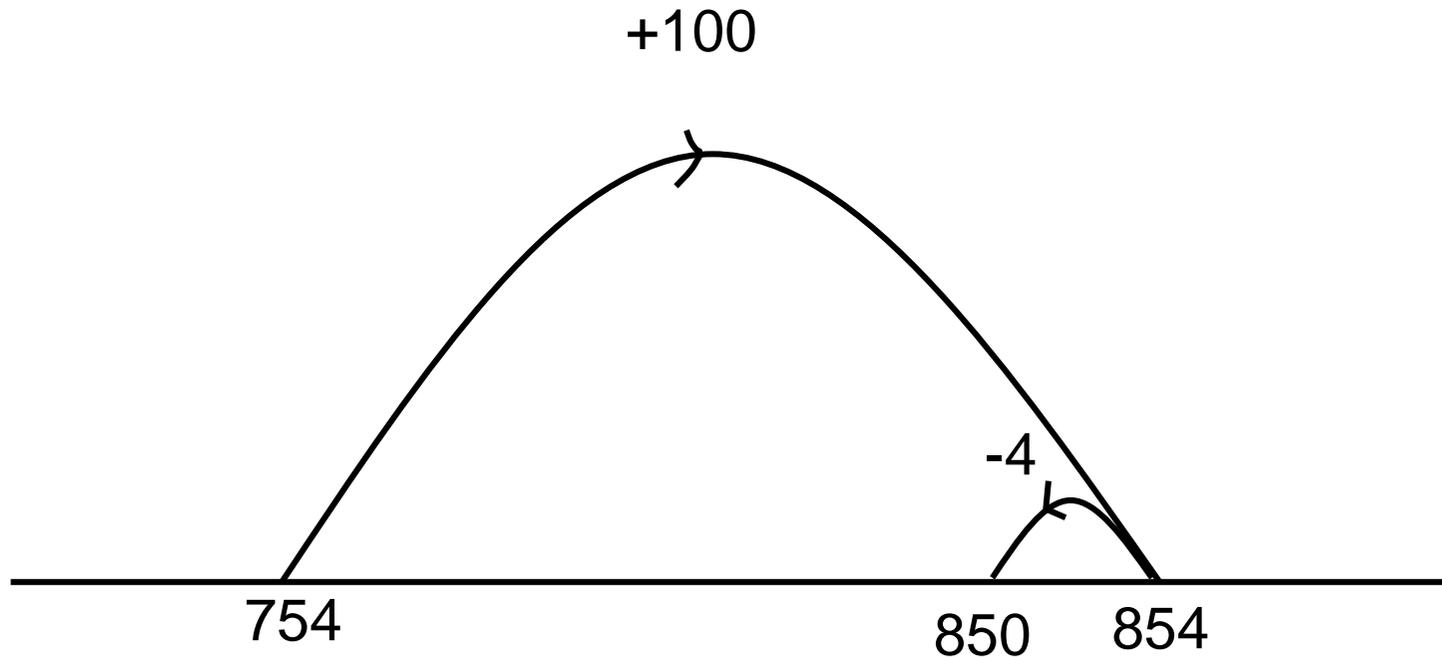


010 – Example

HTU +
TU



Start with the larger number 754. Add on 100 and then subtract 4.



$$754 + 96 =$$

Progression from Mental Maths

- Mental method, using partitioning

Partition into hundreds, tens and ones and recombine

Either partition both numbers and recombine or partition the second number only e.g.

$$358 + 73 = 358 + 70 + 3$$

$$= 428 + 3$$

$$= 431$$

HTU + TU

$$358 + 73 = 358 + 70 + 3$$

$$= 428 + 3$$

$$= 431$$

Mental methods involve **partitioning** the numbers, then adding the tens and the units separately.

ADDITION

Expanded method: moving on from adding the *most significant digits* first to adding *least significant digits* first

HTU +
TU

Why switch to adding the units (*least significant digits*) first?

I know that I can add numbers in any order and the total will be the same. My teacher has told me that I need to practise adding the units first. The next method I will learn works this way. I must remember to line the numbers up in the correct columns.



HTU +
HTU

Add *most significant*
digits first:
(in this example,
hundreds)

$$\begin{array}{r} \text{HTU} \\ 625 \\ + 148 \\ \hline 700 \quad 600 + \\ 60 \quad 100 \\ 13 \\ \hline 773 \end{array}$$

Mentally add
 $700 + 60 + 13 = 773$

Add *least significant*
(in this example,

$$\begin{array}{r} \text{HTU} \\ 625 \\ + 148 \\ \hline 13 \quad 5 + 8 \\ 60 \quad 20 + 40 \\ 700 \quad 600 + 100 \\ \hline 773 \end{array}$$

$$625 + 148 =$$

Leading to



ADDITION

Using the compact method

HTU + HTU
587 + 475

Why do you say
 $80 + 70$ instead of
 $8 + 7$?

I need to remember the
value of each digit, so I
know the size of the
numbers I am adding and
whether my answer
makes sense.



HTU + HTU
587 + 475

HTU
587
+

7 + 5 = 12
Place the **2** in the units column and repartition the **10** to the tens column.

80 + 70 = 150 then + **10** (carried forward) which totals **160**.
Place **60** in the tens column and repartition the **100** forward to the hundreds column.

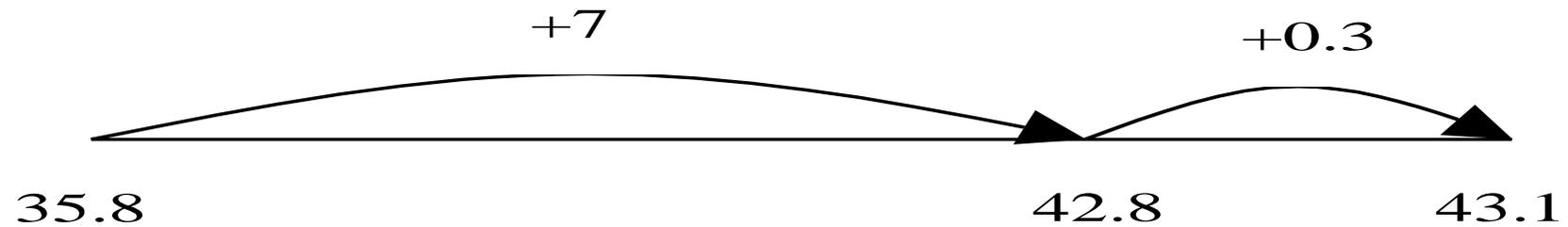
500 + 400 = 900 then + **100** which totals **1000**. Place this in the thousands column.

587 + 475 =

Using a number line to add decimals

Either partition both numbers and recombine or partition the second number only e.g.

$$\begin{aligned} 35.8 + 7.3 &= 35.8 + 7 + 0.3 \\ &= 42.8 + 0.3 \\ &= 43.1 \end{aligned}$$



Using the compact method to add decimals

$$13.86 + 9.481 = 23.341$$

TU. t h th

$$\begin{array}{r}
 13.86 \\
 + 9.481 \\
 \hline
 23.341 \\
 \hline
 \end{array}$$

1 1 1

$$0 + 0.1 = 0.1$$

Place the 1 in the thousandths column.

$$0.06 + 0.08 = 0.14$$

Place the 4 in the hundredths column and repartition the 1 to the tenths column

$10 + 0 = 10$
then add 10
Place in the
tens column

$3 + 9 = 12$ then add 1
Place the 3 in the
column method and
repartition the 1 to the
tens column

$$0.8 + 0.4 = 1.2$$
 then add 0.1

Place the 1 in the tenths column and
repartition the 1 into the units column

End of Year Objectives for Addition

Yr1 – recall and jottings for $U+U$, $T+U$, $T+T$, $TU+U$ (within 20 including 0)

Yr2 – $TU+U$, $T+TU$, $TU+TU$, $U+U+U$

Yr3 – mental methods for $HTU + U$, $HTU+T$, $HTU+H$; written methods for $HTU+TU$, $HTU+HTU$

Yr4 – written methods as above and $ThHTU+ThHTU$, $U.t+U.t$, $£U.th+£U.th$

Yr5 – written method for addition of numbers with more than four digits; 2 or more integers, decimals with 2dp e.g. $29.78 + 54.34$

Yr6 – As above

Differentiation Steps for each Stage:

- Not crossing tens
- Crossing Tens
- Crossing Hundreds Only
- Crossing Tens and Hundreds

In addition:

- The number line must be modeled as an image to support calculation from Reception to Year 6
- Jottings must be modelled as a clear image/strategy for mental calculation
- If the calculation can be carried out mentally then do not give it to practice vertical calculation e.g. $TU + TU$ should not be calculated vertically

Always present calculations horizontally in order to consider mental calculations first.

SUBTRACTION

PREREQUISITE SKILLS:

Prerequisite skills (based on the practical)
Number bonds to 10



Counting back from 20

Find one less than a given number



Subtract using quantities and objects 2 single digit numbers



Count back to subtract single digit numbers



Understand subtraction as 'take away'



There are two concepts linked to subtraction:

Subtract - where it is natural to count back to 'take away'

Find the difference – where the understanding of the vocabulary leads to using addition to count on

SUBTRACTION

Use a number line to count on from the smallest number to the largest number

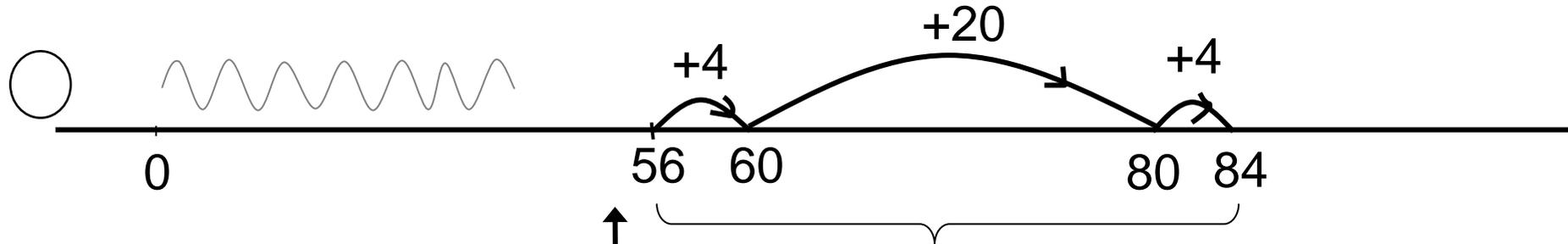
$$\begin{array}{r} \text{TU} - \text{TU} \\ 84 - 56 \end{array}$$

Why do you count on for a subtraction question?

Counting on a number line is easier than taking away, especially if the numbers are close together like $203 - 198$.



TU - TU
84 - 56

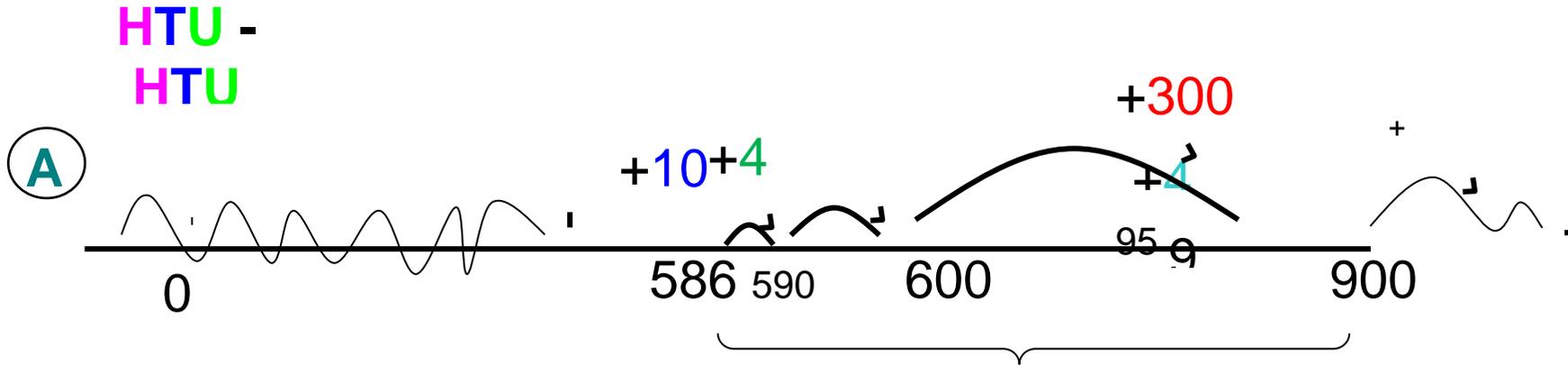


Start by 'taking away' (crossing out) the 56.

START
HERE

Find the *difference* between the two numbers. Count on from 56 to 84.
 $20 + 4 + 4 = 28$

$84 - 56 = 28$



**START
HERE**

'Take away' the 586



Find the *difference* between the two numbers.
Count on from 586 to 954.
 $300 + 50 + 10 + 4 + 4 = 368$

SUBTRACTION

Working towards a standard method

$$\begin{array}{r} \text{HTU} - \text{TU} \\ 154 - 37 \end{array}$$

Why do you need to rearrange the numbers $50 + 4$ and rewrite them as $40 + 14$?

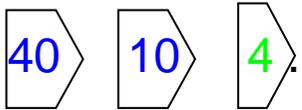
The whole number is 154. It is possible to subtract 7 but for this method I need to do one subtraction in each column. So I exchange one ten from the tens column for ten ones in the units column.



HTU -
TU

Both these numbers are partitioned into their HTU parts, so we can do 3 easier calculations.

54 is the same value as



Now 7 can be subtracted from 14.

Subtract the units, tens, then hundreds.

$$100 - 0 =$$

$$40 - 30 =$$

$$14 - 7 =$$

$$\begin{array}{r} 100 + 50 + 4 \\ - \quad 30 + 7 \end{array}$$

$$\begin{array}{r} 100 + 40 + 10 + 4 \\ - \quad 30 + 7 \end{array}$$

$$\begin{array}{r} 100 + 40 + 14 \\ - \quad 30 + 7 \end{array}$$

$$100 + 10 + 7 =$$

Here the answers from each calculation are added to give the answer.

$$154 - 37 =$$

SUBTRACTION

HTU - HTU
754 - 286

Standard method

Why didn't you
use the standard
method straight
away?

Because all the stages I
have learnt before have
really helped me
understand exactly
what I'm doing.



HTU -
HTU

54 is the same value as
 $\boxed{40} + \boxed{10} + \boxed{4}$.
 Now 6 can be subtracted
 from 14.

740 is the same value
 as $\boxed{600} + \boxed{100} + \boxed{40}$.
 Now 80 can be
 subtracted from 140.

Or, more efficiently
 the *standard method*.

$$\begin{array}{r} 141 \\ \cancel{7}5 \\ 4 \end{array}$$

$$\begin{array}{r} 40 \\ 700 + \cancel{50} + 4 \\ - 200 + 80 + 6 \end{array}$$

$$\begin{array}{r} 60 \\ \cancel{700} + 40 + 14 \\ - 200 + 80 + 6 \end{array}$$

$$\begin{array}{r} 600 + 140 + \\ - 200 + 80 + \\ \hline 400 + 60 + 8 \end{array}$$

$$754 - 286 = 468$$

End of Year Objectives for Subtraction

Year 1 – mentally subtract U-U, TU-U, TU- TU (up to 20 e.g. 15 – 12)

Year 2 - mentally TU-U, TU-multiple of 10, mentally with informal jottings TU-TU

Year 3 – subtract mentally, HTU – U, HTU – T, HTU – H, TU-U, TU-TU. Formal written methods for TU-TU, HTU-TU, HTU-HTU

Year 4 – as above and efficient written methods for ThHTU-ThHTU, ThHTU-HTU, U.t – U.t, £U.th-£U.th

Year 5 – Efficient written methods for subtraction of 2 integers with more than 4 digits e.g. 45230 - 12432 and decimals with up to 2dp e.g. 54.34-29.78

Year 6 – as above

Please note:

There are two concepts linked to subtraction:

Subtract - where it is natural to count back to 'take away'

Find the difference – where the understanding of the vocabulary leads to using addition to count on [complementary addition].

- Children should not move on to a written method if they are not completely confident with using a number line.
- Children will need to have had experience of different types of jumping on a number line e.g. T10 (target the ten), J10 (jump in 10s) and know how to partition numbers in different ways.
- These methods can also be easily applied, at different levels, to finding differences in values of money, measures and time.

Always present calculations horizontally in order to consider mental calculations first.

MULTIPLICATION

Prerequisite skills

Multiplication is related to known facts including doubling and counting groups of the same size.



$$3 + 3$$

E.g. use of dominoes and dice.

Counting using a variety of practical resources



Numicon and bead strings



Counting in 2s e.g. counting socks, shoes, animal's legs...

Counting in 5s e.g. counting fingers, fingers in gloves, toes...

Counting in 10s e.g. fingers, toes...

MULTIPLICATION

Introduction to Multiplication

Multiplication is repeated addition

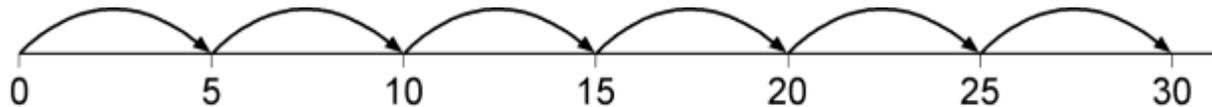
For example:

$$5 \times 6 = 30$$

Which is the same as

$$5 + 5 + 5 + 5 + 5 + 5 = 30$$

We can use a number line to show the repeated addition and work out the answer.

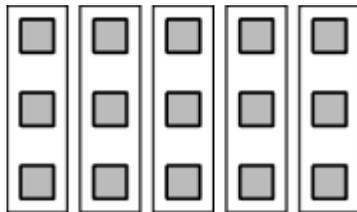


MULTIPLICATION

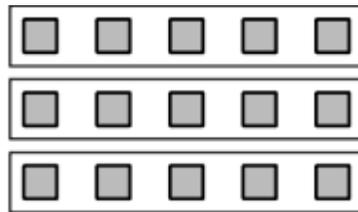
Using arrays to support multiplication

An array is objects or shapes that are arranged in a rectangle. Arrays are very important in helping children understand how multiplication works.

They learn that in the array the answer is always the same (eg 3×5 is the same as 5×3), even when you rotate.



3×5



5×3

MULTIPLICATION

Introducing multiplication on a number line

$$\begin{array}{r} \text{TU X U} \\ 14 \times 5 \end{array}$$

How is multiplication the same as repeated addition?

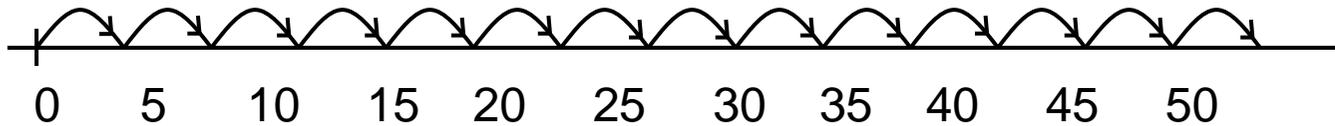
The number line helps me see each group of 5 clearly.

If I add 5 fourteen times, that is the same as 5 multiplied by 14 (5×14). I can make 14 individual jumps of 5 along the number line, or 1 jump of 5×10 and 1 jump of 5×4 . Table facts will help me do this more quickly.

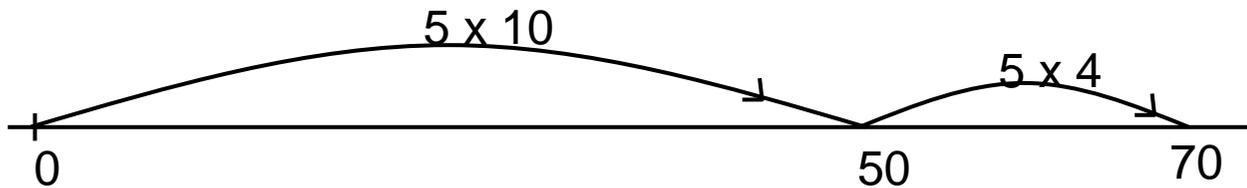


TU x U
14 x 5

The number line shows 5 multiplied by 14. This is equal to 14 multiplied by 5 (14 jumps of 5 on the number line).



Multiplication is *repeated addition*.



Using table facts to make bigger jumps is more efficient.

14 x 5 = 70

GRID

TU X U
14 x 5

Why do you
partition the
numbers into
tens and units?

It doesn't take
long!
I can see what I
have to multiply
very easily.



TU x U

14 x 5

Partition TU number into tens and units parts.
14 becomes 10 and 4

14	10	4
5	50	20

70

$$50 + 20 = 70$$

50 comes from multiplying 10 by 5.

20 comes from multiplying 4 by 5.

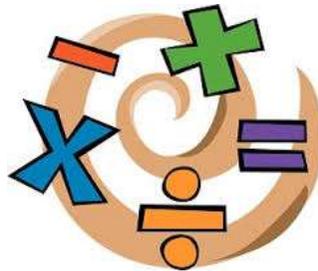
$$14 \times 5 = 70$$

GRID

$$\begin{array}{r} \text{TU} \times \text{TU} \\ 46 \times 32 \end{array}$$

Isn't it difficult to multiply 40 by 30?

I know that 30 is 3×10 and multiplying by 10 is easy so I do $40 \times 3 \times 10 = 120 \times 10 = 1200$.



You've got to do a lot of calculations – don't you get confused?

The layout of the grid helps me organise what I have to do. I like this method.

Both numbers are *partitioned* into their tens and units parts,

46 becomes 40 and 6 and 32 becomes 30 and 2.

46 x 32

	X	40	6	
30		1200	180	1380
2		80	12	+ 92
				1472

The *part products* are added in stages to give the final *product* or answer of 1472.

46 x 32 = 1472

MULTIPLICATION

Grid method, **Expanded method**
and **Compact method**

TU X U
23 x 8

What are the
brackets for in the
expanded method?

Why do you multiply 3
by 8 first in the
compact method?
In all the other methods
I've noticed that you've
multiplied the tens
number first!

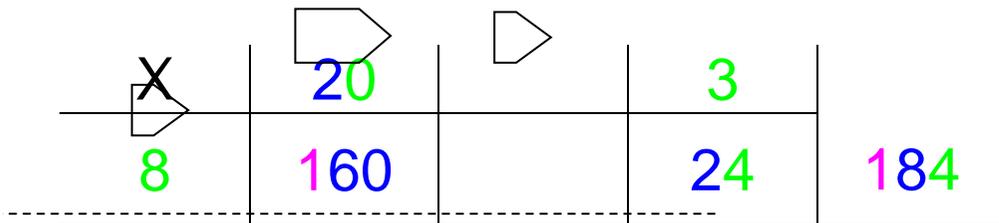
They remind me which numbers I
am multiplying.
I also have to remember to line the
numbers up as hundreds, tens
and units.



I multiply the units
first so I can carry
forward any tens I
need to!
This method is very
quick but I have to
remember to add on
any numbers I carry
forward.

TU X U
23 x 8

GRID



EXPANDED METHOD

20 multiplied by 8 equals 160.

Final product from totalling

$$\begin{array}{r}
 \text{HTU} \\
 23 \\
 \times 8 \\
 \hline
 160 \quad (20 \times 8) \\
 + 24 \quad (3 \times 8) \\
 \hline
 184
 \end{array}$$

COMPACT
T

$$\begin{array}{r}
 \text{HT} \\
 \text{U} \\
 23 \\
 \times 8 \\
 \hline
 \end{array}$$

3 multiplied by 8 equals 24 (the first *part product*).

2 is the 2 tens that need to be carried forward and added to the next *part product*.

20 multiplied by 8 equals 160 (2nd *part product*), plus the 2 tens equals 180.

The digits are put in the correct columns, to give the answer 184.

23 x 8 =
184

MULTIPLICA

Grid method, **Expanded method** and **Compact method**

$$\begin{array}{r} \text{TU} \times \text{TU} \\ 46 \times 32 \end{array}$$

I recognise the long multiplication method. How do you multiply 46 by 30?

Well, I know that 46×30 is the same as $46 \times 3 \times 10$. I know my answer will end in zero when I multiply this whole number by 10. So, I put the zero in first. Then I multiply 46×3 using the short multiplication method.



TU X TU GRID METHOD

X	40	6	
30	1200	180	1380
2	80	12	+ 92
			1472

EXPANDED

The 4 *part products* are set out vertically underneath the calculation.

Part products totalled to give final product.

$$\begin{array}{r}
 46 \\
 \times 32 \\
 \hline
 120 \quad (40 \times 30) \\
 0 \quad (6 \times 30) \\
 180 \quad (40 \times 2) \\
 80 \quad (6 \times 2) \\
 \hline
 \end{array}$$

COMPACT METHOD

$$\begin{array}{r}
 ^1 46 \\
 \underline{\times 32} \\
 92 \\
 1380 \\
 \hline
 \end{array}$$

$$\begin{array}{l}
 2 \times 6 = 12 \\
 2 \times 40 = 80 + \\
 10 \\
 = 90
 \end{array}$$

$$\begin{array}{l}
 30 \times 6 = 180 \\
 30 \times 40 = 120 + \\
 10 = 130
 \end{array}$$

**46 x 32 =
1472**

End of Year Objectives for Multiplication

Year 1—practical problems that combine groups of 2, 5 or 10

Year 2 -represent multiplication as repeated + and arrays. Practical and informal written methods and vocabulary used to support multiplication alongside known facts and mental strategies. Understand and use '3 for free' for \times and \square of the 2, 3,4,5,6, 8 and 10 times-tables.

Year 3 –Describe the effect of $U \times 10$, $TU \times 10$, $U \times 100$, $TU \times 100$. Practical and informal written methods for $TU \times U$.

Year 4 –Derive and recall \times and \div facts up to 12×12 and '3 for free' facts. Multiply numbers to 1000 by 10 and 100. Formal written layout and explain $TU/HTU \times U$.

Year 5 –mentally multiply $TU \times U$. Multiply whole numbers and decimals by 10, 100 and 1000. Formal written methods to multiply $ThHTU \times U$, $ThHTU \times TU$, $U.t \times U$

Year 6 –mentally calculate $TU \times U$, $U.t \times U$. Formal written methods to multiply up to 4 digit by 2 digit and one digit with up to 2 decimal places.

As with addition and subtraction, before progressing through the stages of calculation:

Learning

- It is crucial to know or be able to derive key number facts:
 - ⇒ Understand and use doubling and halving
 - ⇒ $\times/\div 10$ (as moving a place to the left/right NOT "add a zero" etc.!!)
- Place value and partitioning MUST be clearly understood and explained using the appropriate mathematical vocabulary.

Teaching

- The number line and the use of arrays must be modelled as images to support calculation from Reception to Year 6.
- Jottings must be modelled as a clear image/strategy for mental calculation.
- If the calculation should be possible mentally then do not give it to practise vertical calculation, e.g. 23×15 should not be calculated vertically. Consider use of numbers carefully.

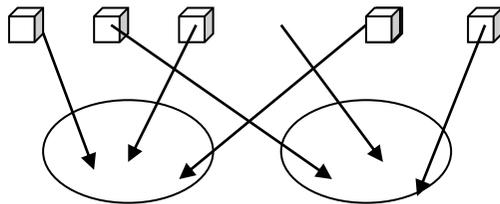
Always present calculations horizontally in order to consider mental calculations first

DIVISION

Sharing objects equally

SHARING equally occurs when a quantity is shared out equally into a given number of portions, and we can work out how many are in each portion.

E.g. $6 \div 2$ (share 6 sweets between 2 children)



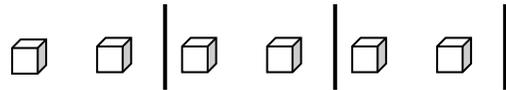
Sharing can be carried out using practical apparatus, such as cubes.

If children only understand the sharing model of subtraction they will need very good knowledge of tables in order to carry out division

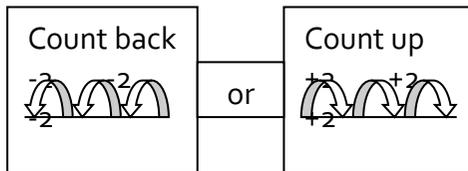
GROUPING (or repeated subtraction) occurs when we are asked to find how many groups of a given size are equivalent to the original quantity. For example how many groups of 2 marbles are in a set of 6 marbles, the calculation

$$6 \div 2 \quad (\text{how many 2s in 6?})$$

Vocabulary → divided into groups of



Shown/calculated on a number line:



- ***KS1 tends to focus on “sharing” because this is a word and a concept that children understand and also it is the picture suggested by halving.***

DIVISION

Introducing division on a number line

TU \div U

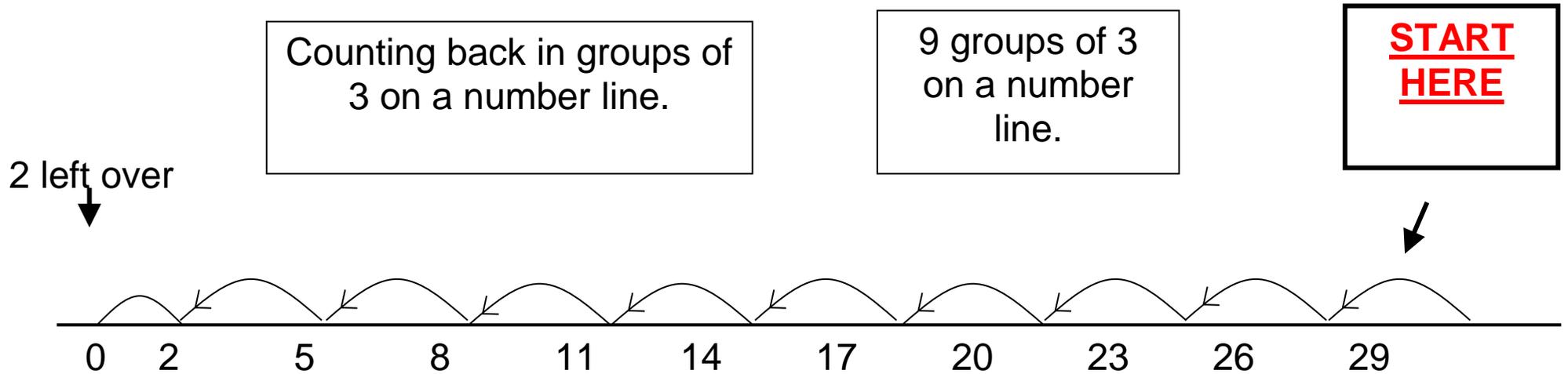
29 \div 3

Why are you adding on one line and subtracting on the other? And what has subtraction got to do with division?

I need to see how many groups of 3 there are in 29, so I either add on or take away groups of 3 until I can't add or take any more. Using the subtraction method will help me later on.



$$\begin{array}{r} \text{TU} \div \\ \text{II} \end{array}$$



There are 9 groups of 3 in 29, with 2 left over.

$$29 \div 3 = 9r2$$

DIVISION

Chunking on a number line

TU \div U

72 \div 5

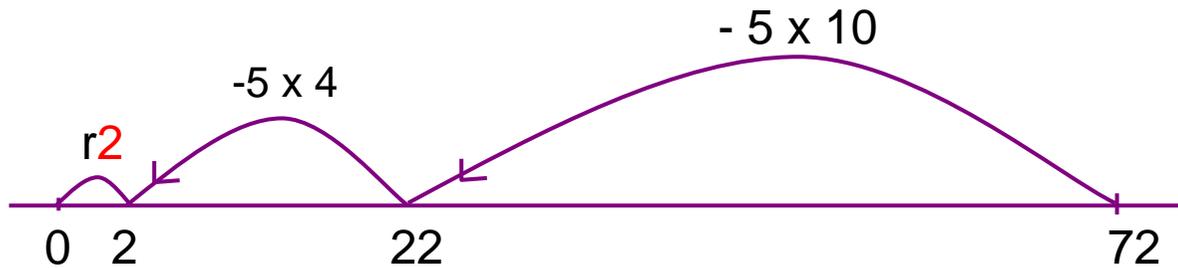
I've never heard of chunking before!
How does this help with division?

If I can, I try to take out 10 groups of the number I'm dividing by. This is a big chunk and makes the calculation easier. But I can take out chunks that are any number of groups.



$$TU \div U$$

$$72 \div 5$$



Subtract 4 groups of 5 (20) from 22 to land on 2.

Subtract 10 groups of 5 (50) from 72 to land on 22.

START
HERE

14 groups of 5 subtracted altogether.

2 left!
This is the *remainder*.

$$72 \div 5 =$$

DIVISION BY

HTU \div U

$$256 \div 7$$

How do you
decide what
size chunk to
subtract?

I look for chunks of 10 first. If I
take bigger chunks it makes the
calculation quicker and easier.
Method **C** is shorter and more
efficient than **B** .



How many groups of 7 in 256?

HTU ÷ **U**
256 ÷ **7**

$$\begin{array}{r} 256 \\ -70 \text{ (7 x 10)} \\ \hline 186 \\ -70 \text{ (7 x 10)} \\ \hline 116 \\ -70 \text{ (7 x 10)} \\ \hline 46 \\ -42 \text{ (7 x 6)} \\ \hline 4 \end{array}$$

Subtract
chunks of 70 (7
x 10).

How many
groups of 7 in
46?

Total the numbers of groups of 7.

$$\textcircled{10} + \textcircled{10} + \textcircled{10} + 6 = 36$$

Leading to

$$\begin{array}{r} 256 \\ -210 \text{ (7 x 30)} \\ \hline 46 \\ -42 \\ \hline 4 \end{array} \text{ (7 x 6)}$$

Subtract one large chunk
of 210 (7 x 30).

36 groups of 7 have been
subtracted and there is 4
left over.

$$\mathbf{256 \div 7 = 36r4}$$

SHORT DIVISION

$$\begin{array}{r} \text{HT U} \div \text{U} \\ 432 \div 2 \end{array}$$

$$\begin{array}{r} 216 \\ 2 \overline{)432} \end{array}$$

In order that this method is taught to its best efficiency we first discuss the place value of each digit but then take each digit as a stand alone unit value e.g. 4 rather than 400. It is imperative that children have a secure understanding of place value before progressing to this method as throughout the modelling they may need to explain the true place value of each digit rather than its unit value e.g. 30 rather than 3.

End of Year Objectives for Division

Year 1 –practical problems that share into equal groups of 2, 5 or 10.

Year 2 –derive and recall division facts for 2, 5 or 10, represent division as repeated subtraction (grouping) and sharing. Practical and informal written methods and vocabulary used to support division, including remainders. To know that division is not commutative.

Year 3 –Practical and informal written methods for $TU \div U$. Understand and use ‘3 for free’ for x and \square of the 2, 3, 4, 5, 6, 8 and 10 times-tables. Round remainders up or down, depending on the context.

Year 4 –Derive and recall x facts up to 12×12 and apply ‘3 for free’ facts. Divide numbers to 1000 by 10 and 100. Develop and use formal written layouts to record.

Year 5 –Divide whole numbers and decimals by 10, 100 and 1000. Divide numbers up to 4 digits by a one digit number using the formal written methods for division and interpret remainders appropriately for the context.

Year 6 –Divide numbers up to 4 digits by a 2 digit whole number using the formal written method of long division interpreting remainders as fractions, decimals, etc. Divide numbers up to 4 digits by a two digit number using the formal written methods for division and interpret remainders appropriately for the context.

As with multiplication, before progressing through the stages of calculation:

Learning

- It is crucial to know or be able to derive key number facts:
 - ⇒ Understand and use doubling and halving
 - ⇒ $\times/\div 10$ (as moving a place to the left/right NOT “add a zero” etc.!!)
- Place value and partitioning MUST be clearly understood and explained using the appropriate mathematical vocabulary.

Teaching

- The number line and the use of arrays must be modelled as images to support calculation from Reception to Year 6.
- Jottings must be modelled as a clear image/strategy for mental calculation.
- If the calculation should be possible mentally then do not give it to practise vertical calculation, e.g. $24 \div 3$ should not be calculated using short division. Consider use of numbers carefully.

CALCULATIONS IN

All the methods in this booklet support children in using their mental and written skills to solve calculations. Children need to be encouraged to use the method that they understand and can use confidently.

It is important that children are able to choose the most appropriate method for the calculation. For example:

4003 – 3998 These numbers are very close together and so counting up on a number line (actual or imagined) would be the most efficient method.

200 ÷ 4 Dividing by 4 is the same as halving and halving again. As it is easy to halve 200 and easy to halve 100, this would be the most efficient method.

Using and applying appropriate skills is very important, when calculations are needed to solve a problem.

4 C.DS at £2.99 – how much altogether?

£2.99 is almost £3.00 and so round up, multiply, then adjust:

$$4 \times £3.00 = £12.00$$

$$£12.00 - 4p = £11.96$$